# $\frac{\text{SUMMER}}{m \land + \pi}$

Dear Students and Parents/Guardians,

Welcome to AP Precalculus / Precalculus Honors! We are excited to support your continued advancement in mathematics and help prepare you for a rigorous and rewarding academic year. To ensure that all students are ready for the fast-paced and challenging nature of this course, a summer assignment has been prepared to reinforce and build upon key concepts from Algebra 1 and Algebra 2.

This summer packet is intended to strengthen students' understanding of Algebra 1 and Algebra 2 content, which forms the essential foundation for success in Precalculus. Please be aware that these prerequisite concepts will not be retaught during the course. AP Precalculus and Precalculus Honors are designed to move quickly and cover extensive material, requiring a solid grasp of earlier topics from day one. Completing this work is an important step toward ensuring readiness for these demands.

- Due Date: The completed summer packet is to be submitted on the first day of school.
- Assessment: During the first week of school, students will take an assessment on the material covered in the summer assignment to verify their preparedness. Students who do not demonstrate readiness on this assessment will be placed in an alternative math course better suited to their current level of preparation. Our goal is to ensure that all students are placed in the course that best supports their long-term academic success in mathematics.

#### Academic Integrity – Honor Code:

By signing below, both the student and parent/guardian affirm that:

- The summer assignment was completed independently, without the use of artificial intelligence tools or outside assistance other than tutorial videos/websites.
- A calculator was not used.
- The work submitted reflects the student's own understanding and effort.

# I, the student, affirm that I have completed this summer assignment honestly and independently. I did not use AI tools or a calculator.

Student Name (Print): \_\_\_\_\_\_

Student Signature: \_\_\_\_\_ Date: \_\_\_\_\_

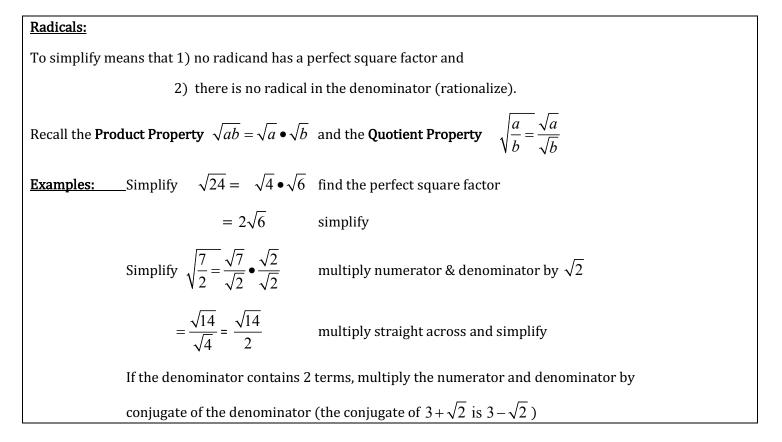
I, the parent/guardian, acknowledge that my child has completed this assignment independently and I understand the expectations for AP Precalculus / Precalculus Honors.

Parent/Guardian Name (Print): \_\_\_\_\_

Parent/Guardian Signature: \_\_\_\_\_ Date: \_\_\_\_\_

We look forward to a challenging and successful year ahead!
Sincerely,
The CCS Mathematics Department

# NO CALCULATOR SHOULD BE USED TO COMPLETE ANY PART OF THIS PACKET.



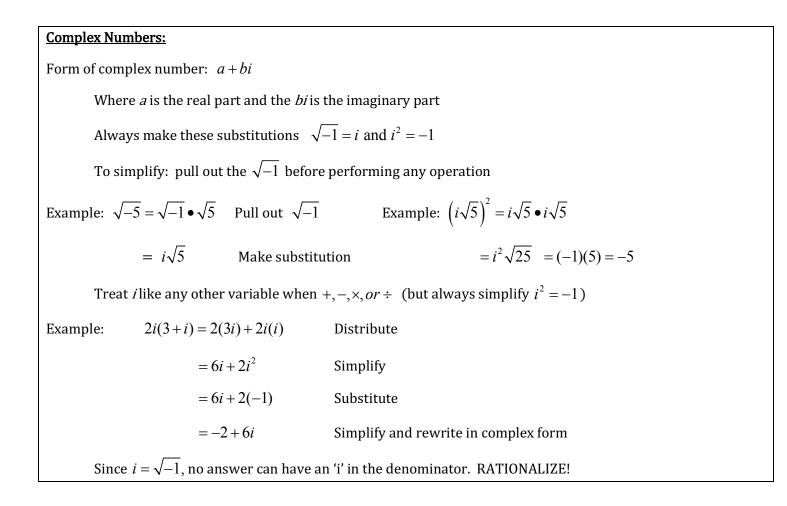
#### Simplify each of the following.

1.  $\sqrt{32}$  2.  $\sqrt{(2x)^8}$  3.  $\sqrt[3]{-64}$  4.  $\sqrt{49m^2n^8}$ 

5. 
$$\sqrt{\frac{11}{9}}$$
 6.  $\sqrt{60} \bullet \sqrt{105}$  7.  $(\sqrt{5} - \sqrt{6})(\sqrt{5} + \sqrt{2})$ 

#### Rationalize.

8. 
$$\frac{1}{\sqrt{2}}$$
 9a.  $\frac{2}{\sqrt{3}}$  10a.  $\frac{3}{2-\sqrt{5}}$ 



Simplify.

9b.  $\sqrt{-49}$  10b.  $6\sqrt{-12}$  11. -6(2-8i)+3(5+7i)

12. 
$$(3-4i)^2$$
 13.  $(6-4i)(6+4i)$ 

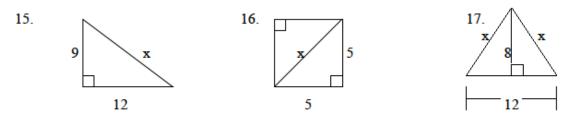
#### Rationalize.

14.  $\frac{1+6i}{5i}$ 

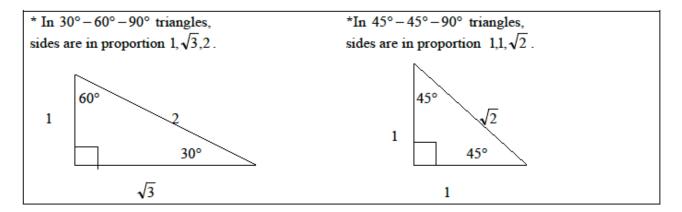
#### Geometry:

Pythagorean Theorem (right triangles):  $a^2 + b^2 = c^2$ 

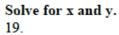
# Find the value of x.

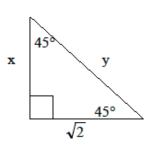


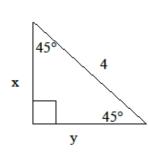
18. A square has perimeter 12 cm. Find the length of the diagonal.

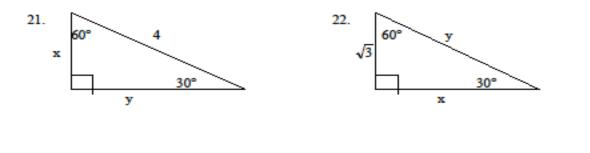


20.









Equations of Lines:		
Slope-intercept form: $y = mx + b$	Vertical line: $x = c$	(slope is undefined)
Point-slope form: $y - y_1 = m(x - x_1)$	Horizontal line: $y = c$	(slope is zero)
Standard Form: $Ax + By = C$	Slope: $m = \frac{y_2 - y_1}{x_2 - x_1}$	

23. State the slope and y-intercept of the linear equation: 5x - 4y = 8

24. Find the x-intercept and y-intercept of the equation: 2x - y = 5

25. Write the equation in standard form: y = 7x - 5

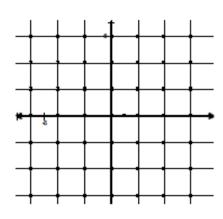
#### Write the equation of the line in slope-intercept form with the following conditions:

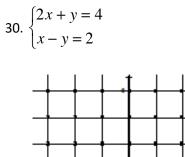
- 26. slope = -5 and passes through the point (-3, -8)
- 27. passes through the points (4, 3) and (7, -2)

28. x-intercept = 3 and y-intercept = 2

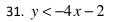
<u>Graphing:</u> Graph each function, inequality, and/or system.

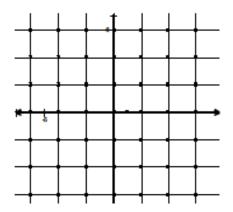
29. 
$$3x - 4y = 12$$



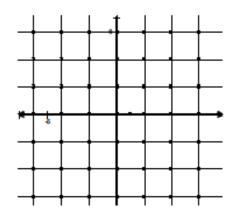




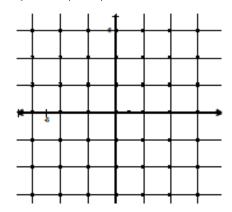




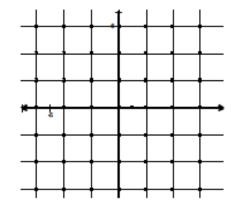
33. y > |x| - 1



32. y + 2 = |x + 1|



34. 
$$y + 4 = (x - 1)^2$$



# Systems of Equations:

$$\begin{cases} 3x + y = 6 \\ 2x - 2y = 4 \end{cases}$$

$\left(2x-2y-4\right)$			
Substitution:		Elimination:	
Solve 1 equation for 1	variable	Find opposite	coefficients for 1 variable
Rearrange.		Multiply equa	tion(s) by constant(s).
Plug into 2 <sup>nd</sup> equation	l.	Add equations	s together (lose 1 variable)
Solve for the other va	riable.	Solve for varia	able.
Then plug answer back into an original equation to solve for the 2 <sup>nd</sup> variable.			
y = 6 - 3x	Solve $1^{st}$ equation for y	6x + 2y = 12	Multiply 1 <sup>st</sup> equation by 2
2x-2(6-3x)=4	Plug into $2^{nd}$ equation	2x - 2y = 4	coefficients of y are opposite
2x - 12 + 6x = 4	Distribute	8x = 16	Add
8x = 16 and $x = 2$	Simplify	<i>x</i> = 2	Simplify.
Plug x=2 back into the original equation $\begin{cases} 6+y=6\\ y=0 \end{cases}$			

Solve each system of equations, using any method.

$$35. \begin{cases} 2x + y = 4\\ 3x + 2y = 1 \end{cases}$$

$$36. \begin{cases} 2x + y = 4\\ 3x - y = 14 \end{cases}$$

37. 
$$\begin{cases} 2w - 5z = 13\\ 6w + 3z = 10 \end{cases}$$

# Exponents:

# Recall the following rules of exponents:

1.	$a^1 = a$	Any number raised to the power of one equals itself.
2.	$1^{a} = 1$	One raised to any power is one.
3.	$a^{0} = 1$	Any nonzero number raised to the power of zero is one.
4.	$a^m \cdot a^n = a^{m+n}$	When multiplying two powers that have the same base, add the exponents.
5.	$\frac{a^m}{a^n} = a^{m-n}$	When dividing two powers with the same base, subtract the exponents.
6.	$(a^m)^n = a^{mn}$	When a power is raised to another power, multiply the exponents.
7.	$a^{-n} = \frac{1}{a^n}$ and	$\frac{1}{a^{-n}} = a^n$ Any nonzero number raised to a negative power equals its reciprocal raised
		to the opposite positive power.

# Express each of the following in simplest form. Answers should not have any negative exponents.

38. 
$$5a^{0}$$
  
39.  $\frac{3c}{c^{-1}}$   
40.  $\frac{2ef^{-1}}{e^{-1}}$   
41.  $\frac{(n^{3}p^{-1})^{2}}{(np)^{-2}}$   
Simplify.  
42.  $3m^{2} \cdot 2m$   
43.  $(a^{3})^{2}$   
44.  $(-b^{3}c^{4})^{5}$   
45.  $4m(3a^{2}m)$ 

# Polynomials:

To add/subtract polynomials, combine like terms.

EX:	8x - 3y + 6 - (6y + 4x - 9)	Distribute the negative through the parantheses.
	=8x-3y+6-6y-4x+9	Combine like terms with similar variables.
	= 8x - 4x - 3y - 6y + 6 + 9	
	=4x-9y+15	

Simplify.

46.  $3x^3 + 9 + 7x^2 - x^3$  47. 7m - 6 - (2m + 5)

To m	ultiply two binomials, use FOIL.	
EX:	(3x-2)(x+4)	Multiply the first, outer, inner, and last terms.
	$=3x^{2}+12x-2x-8$	Combine like terms together.
	$=3x^{2}+10x-8$	

# Multiply.

48. (3a+1)(a-2)

49. (s+3)(s-3)

50.  $(c-5)^2$ 

51. (5x+7y)(5x-7y)

#### **Factoring:**

Follow these steps in order to factor polynomials.

**STEP 1:** Look for a GCF in ALL of the terms.

a) If you have one (other than 1) factor it out.

b) If you don't have one move on to STEP 2

**STEP 2:** How many terms does the polynomial have?

**2 Terms** a) is it the difference of two squares?  $a^2 - b^2 = (a+b)(a-b)$ 

**EX:**  $x^2 - 25 = (x+5)(x-5)$ 

b) Is it the sum or difference of two cubes? 
$$\frac{a^3 - b^3 = (a - b)(a^2 + ab + b^2)}{a^3 + b^3 = (a + b)(a^2 - ab + b^2)}$$

EX: 
$$\frac{m^3 + 64 = (m+4)(m^2 - 4m + 16)}{p^3 - 125 = (p-5)(p^2 + 5p + 25)}$$

3 Terms

EX:

$x^{2} + bx + c = (x + )(x + )$	$x^2 + 7x + 12 = (x+3)(x+4)$
$x^{2}-bx-c = (x-)(x-)$	$x^2 - 5x + 4 = (x - 1)(x - 4)$
$x^{2} + bx - c = (x - )(x + )$	$x^2 + 6x - 16 = (x - 2)(x + 8)$
$x^{2}-bx-c = (x-)(x+)$	$x^2 - 2x - 24 = (x - 6)(x + 4)$

- 4 Terms---Factor by Grouping
- a) Pair up first two terms and last two terms.
- b) Factor out GCF of each pair of numbers.
- c) Factor out front parentheses that the terms have in common.
- d) Put leftover terms in parentheses.

$$Ex: x^{3} + 3x^{2} + 9x + 27 = (x^{3} + 3x^{2}) + (9x + 27)$$
$$= x^{2}(x+3) + 9(x+3)$$
$$= (x+3)(x^{2}+9)$$

# Factor completely.

52. $z^2 + 4z - 12$	53. $6-5x-x^2$	54. $2k^2 + 2k - 60$
$101^4$ 151 <sup>2</sup>	$5 < 0^{2} \cdot 20 \cdot 25$	$\mathbf{r}$
55. $-10b^4 - 15b^2$	56. $9c^2 + 30c + 25$	57. $9n^2 - 4$

To solve quadratic equations, try to factor first and set each factor	equal to zero. Solve for your variable. If the
quadratic does NOT factor, use the quadratic formula.	

EX:	$x^2 - 4x = 21$	Set equal to zero FIRST.
	$x^2 - 4x - 21 = 0$	Now factor.
	(x+3)(x-7) = 0	Set each factor equal to zero.
	x+3=0  x-7=0	Solve for each x.
	$x = -3 \qquad x = 7$	

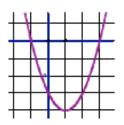
# Solve each equation.

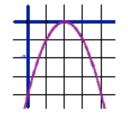
**Discriminant:** The number under the radical in the quadratic formula  $(b^2 - 4ac)$  can tell you what kind of roots you will have.

If  $b^2 - 4ac > 0$  you will have TWO real roots

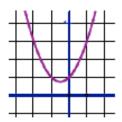
If  $b^2 - 4ac = 0$  you will have ONE real root (touches axis once)

(touches the x-axis twice)





If  $b^2 - 4ac < 0$  you will have TWO imaginary roots. (Function does not cross the x-axis)



QUADRATIC FORMULA—allows you to solve any quadratic for all its real and imaginary roots.

 $5x^2 - 2x + 4 = 0 \ x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ 

EX: In the equation  $x^2 + 2x + 3 = 0$ , find the value of the discriminant, describe the nature of the roots, then solve.  $x^2 + 2x + 3 = 0$  Determine the values of a, b, and c. a = 1 b = 2 c = 3 Find the discriminant.  $D = 2^2 - 4 \cdot 1 \cdot 3$  D = 4 - 12 D = -8 There are two imaginary roots. Solve:  $x = \frac{-2 \pm \sqrt{-8}}{2}$   $x = \frac{-2 \pm 2i\sqrt{2}}{2}$  $x = -1 \pm i\sqrt{2}$ 

Find the value of the discriminant, describe the nature of the roots, then solve each quadratic. Use EXACT values.

63.  $x^2 - 9x + 14 = 0$  64.  $5x^2 - 2x + 4 = 0$ 

Discriminant =	Discriminant =
Type of Roots:	Type of Roots:
Exact Value of Roots:	Exact Value of Roots:

<u>Synthetic Division</u>—can ONLY be used when dividing a polynomial by a linear polynomial.

<b>EX:</b> $\frac{2x^3 + 3x^2 - 6x + 10}{x + 3}$	
Long Division	Synthetic Division
$\frac{2x^3 + 3x^2 - 6x + 10}{x + 3}$	$\frac{2x^3 + 3x^2 - 6x + 10}{x + 3}$
$2x^{2}-3x+3+\frac{1}{x+3}$ $x+3) \qquad 2x^{3}+3x^{2}-6x+10$ $(-)(2x^{3}+6x^{2})$	$\frac{2x^3 + 3x^2 - 6x + 10}{x + 3}$ -3 2 3 -6 10
$-3x^2-6x$	-6 9 -9
$(-)\left(-3x^2-9x\right)$	2 -3 3 1
3x + 10	$= 2x - 3x + 3 + \frac{1}{x + 3}$
(-) (3x+9)	
1	

Divide each polynomial using long division OR synthetic division.

65. 
$$\frac{c^3 - 3c^2 + 18c - 16}{c^2 + 3c - 2}$$
66. 
$$\frac{x^4 - 2x^2 - x + 2}{x + 2}$$

To evaluate a function for the given value, simply plug the value into the function for x.

#### Evaluate each function for the given value.

67. 
$$f(x) = x^2 - 6x + 2$$
 68.  $g(x) = 6x - 7$ 
 69.  $f(x) = 3x^2 - 4$ 
 $f(3) = \_\_\_$ 
 $g(x+h) = \_\_\_$ 
 $5[f(x+2)] = \_\_\_$ 

**Composition and Inverses of Functions:** 

**Recall:**  $(f \ g)(x) = f(g(x)) \operatorname{OR} f[g(x)]$  read "**f** of **g** of **x**" means to plug the inside function in for x in the outside function.

**Example:** Given  $f(x) = 2x^2 + 1$  and g(x) = x - 4 find f(g(x)).

f(g(x)) = f(x-4)= 2(x-4)<sup>2</sup>+1 = 2(x<sup>2</sup>-8x+16)+1 = 2x<sup>2</sup>-16x+32+1 f(g(x)) = 2x<sup>2</sup>-16x+33

**Suppose** f(x) = 2x, g(x) = 3x - 2, and  $h(x) = x^2 - 4$ . Find the following:

70. f[g(2)] =\_\_\_\_\_ 71. f[g(x)] =\_\_\_\_\_

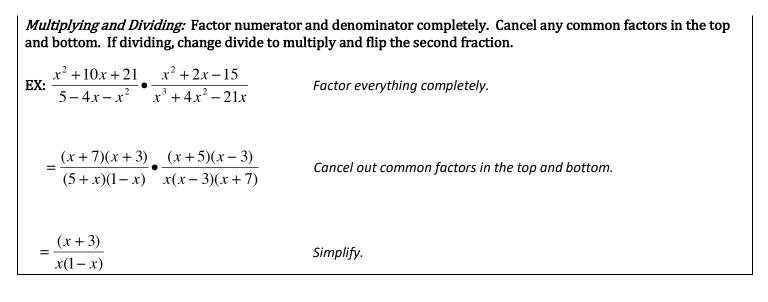
72. f[h(3)] =\_\_\_\_\_

73. g[f(x)] =\_\_\_\_\_

Example:	$f(x) = \sqrt[3]{x+1}$	Rewrite $f(x)$ as y
	$y = \sqrt[3]{x+1}$	Switch x and y
	$x = \sqrt[3]{y+1}$	Solve for your new <i>y</i>
	$\left(x\right)^{3} = \left(\sqrt[3]{y+1}\right)^{3}$	Cube both sides
	$x^3 = y + 1$	Simplify
	$y = x^3 - 1$	Solve for <i>y</i>
	$f^{-1}(x) = x^3 - 1$	Rewrite in inverse notation
Find the inverse, $f^{-1}(x)$ , if possible.		

74. f(x) = 5x + 2

75. 
$$f(x) = \frac{1}{2}x - \frac{1}{3}$$



**76.** 
$$\frac{5z^3 + z^2 - z}{3z}$$
 **77.**  $\frac{m^2 - 25}{m^2 + 5m}$  **78.**  $\frac{10r^5}{21s^2} \bullet \frac{3s}{5r^3}$ 

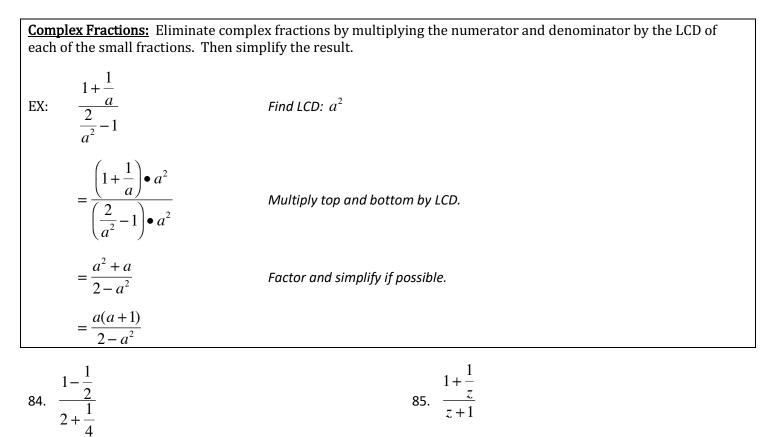
70	$a^2 - 5a + 6$	3a + 12	6d-9, $6-1$	$13d + 6d^2$
79.	a+4	a-2	<b>80.</b> $\frac{1}{5d+1} - \frac{1}{15d}$	$\frac{1}{2} - 7d - 2$

Addition and Subtraction

First find the least common denominator. Write each fraction with that LCD. Add/subtract numerators as indicated and leave the denominators as they are.

$\frac{3x+1}{x(x+2)} + \frac{5x-4}{2(x+2)}$ Find LCD, which is $(2x)(x+2)$ $\frac{2(3x+1)}{2x(x+2)} + \frac{x(5x-4)}{2x(x+2)}$ Rewrite each fraction with the LCD in the denominator. $\frac{6x+2+5x^2-4x}{2x(x+2)}$ Write as one fraction. $\frac{5x^2+2x+2}{2x(x+2)}$ Combine like terms.	EX:	$\frac{3x+1}{x^2+2x} + \frac{5x-4}{2x+4}$	Factor denominator completely.
$\frac{6x+2+5x^2-4x}{2x(x+2)}$ Write as one fraction. $\frac{5x^2+2x+2}{2x(x+2)}$ Combine like terms		$\frac{3x+1}{x(x+2)} + \frac{5x-4}{2(x+2)}$	Find LCD, which is $(2x)(x+2)$
$\frac{2x(x+2)}{5x^2+2x+2}$ Write as one fraction. $\frac{5x^2+2x+2}{5x^2+2x+2}$ Combine like terms		$\frac{2(3x+1)}{2x(x+2)} + \frac{x(5x-4)}{2x(x+2)}$	Rewrite each fraction with the LCD in the denominator.
Combine like terms			Write as one fraction.
2x(x+2)		$\frac{5x^2 + 2x + 2}{2x(x+2)}$	Combine like terms.

2x x	b-a + a+b	$2-a^2 + 3a+4$
81. $\frac{-1}{5} - \frac{1}{3}$	82. $\frac{a^2b}{a^2b} + \frac{ab^2}{ab^2}$	83. $\frac{1}{a^2 + a} + \frac{1}{3a + 3}$





87. 
$$\frac{2 + \frac{1}{x} - \frac{1}{x^2}}{1 + \frac{4}{x} + \frac{3}{x^2}}$$

#### **Solving Rational Equations:**

Multiply each term by the LCD of all the fractions. This should eliminate all of our fractions. Then solve the equation as usual.

$$\frac{5}{x+2} + \frac{1}{x} = \frac{5}{x}$$
Find LCD first  $x(x+2)$ 

$$x(x+2)\frac{5}{x+2} + x(x+2)\frac{1}{x} = \frac{5}{x}x(x+2)$$
Multiply each term by the LCD.
$$5x + 1(x+2) = 5(x+2)$$
Simplify and solve.
$$5x + x + 2 = 5x + 10$$

$$6x + 2 = 5x + 10$$

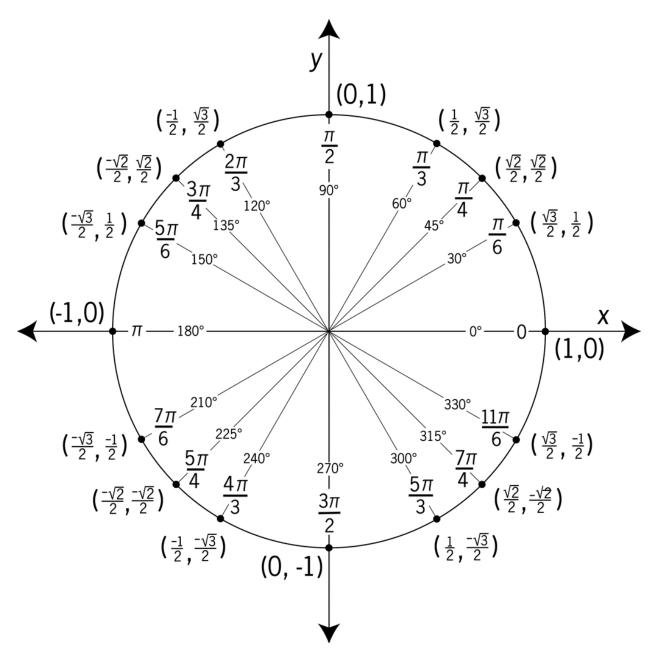
$$x = 8 \quad \leftarrow \text{ Check your answer! Sometimes they do not check!}$$
Check:
$$\frac{5}{8+2} + \frac{1}{8} = \frac{5}{8}$$

$$\frac{5}{10} + \frac{1}{8} = \frac{5}{8}$$

Solve each equation. Check your solutions.

12 3 3	x + 10 = 4	5 x
$88. \ \frac{12}{x} + \frac{3}{4} = \frac{3}{2}$	89. $\frac{x^2 + 2z}{x^2 - 2} = \frac{1}{x}$	90. $\frac{5}{x-5} = \frac{x}{x-5} - 1$
$x$ 4 $\angle$	x = 2 - x	x - 3 $x - 3$

Must COMPLETELY memorize every part of the unit circle. Test on first day of class. Add 360° and  $2\Pi$  to under 0° and 0.



# Summer Review Packet for Pre-Calculus

# Solutions to Odd Exercises

**1.** 
$$4\sqrt{2}$$
  
**3.**  $-4$   
**5.**  $\frac{\sqrt{11}}{3}$   
**7.**  $5 + \sqrt{10} - \sqrt{30} - 2\sqrt{3}$   
**9a.**  $\frac{2\sqrt{3}}{3}$   
**9b.**  $7i$   
**11.**  $3 + 69i$   
**13.**  $52$   
**15.**  $15$   
**17.**  $10$   
**19.**  $\sqrt{2}$   
**21.**  $x=2$   $y=2\sqrt{3}$   
**23.**  $m = \frac{5}{4}$   $b = -2$   
**25.**  $7x - y = 5$   
**27.**  $y = -\frac{5}{3}x + \frac{29}{3}$   
**29.**  $31, 33$  graphs  
**35.**  $(7, -10)$   
**37.**  $\left(\frac{89}{36}, -\frac{29}{18}\right)$   
**39.**  $3c^2$   
**41.**  $n^8$   
**43.**  $a^6$   
**45.**  $12a^2m^2$   
**47.**  $5m - 11$   
**49.**  $s^2 - 9$   
**51.**  $25x^2 - 49y^2$   
**53.**  $-(x + 6)(x - 1)$   
**55.**  $-5b^2(2b^2 + 3)$   
**57.**  $(3n - 2)(3n + 2)$   
**59.**  $2(m + s)(n - t)$   
**61.**  $x = 5$   
**63.**  $25; 2 \ real; 7 \ and 2$   
**65.**  $(c - 6) + \frac{38c - 28}{c^2 + 3c - 2}$   
**67.**  $-7$   
**69.**  $15x^3 + 60x + 40$   
**71.**  $6x - 4$   
**73.**  $6x - 2$   
**75.**  $f^{-1}(x) = 2x + \frac{2}{3}$   
**77.**  $\frac{m-5}{m}$   
**79.**  $3(a - 3)$   
**81.**  $\frac{x}{15}$   
**83.**  $\frac{4a + 6}{3a(a + 1)}$   
**85.**  $\frac{1}{z}$   
**87.**  $\frac{2x - 1}{x + 3}$   
**89.**  $x = 4, -\frac{2}{3}$